



Failure mechanisms and surface roughness statistics of fractured Fontainebleau sandstone

Laurent Ponson, Harold Auradou, Marc Pessel, Veronique Lazarus,
Jean-Pierre Hulin

► To cite this version:

Laurent Ponson, Harold Auradou, Marc Pessel, Veronique Lazarus, Jean-Pierre Hulin. Failure mechanisms and surface roughness statistics of fractured Fontainebleau sandstone. *Physical Review E* , 2007, 76 (3), pp.id. 036108. 10.1103/physRevE.76.036108 . hal-00142793

HAL Id: hal-00142793

<https://hal.science/hal-00142793>

Submitted on 22 Apr 2007

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Failure mechanisms and surface roughness statistics of fractured Fontainebleau sandstone

L. Ponson^{1,*}, H. Auradou^{1,†}, M. Pessel², V. Lazarus^{1,3}, and J.P. Hulin¹

¹ *Laboratoire Fluide, Automatique et Systèmes Thermiques,
UMR No. 7608, CNRS, Université Paris 6 and 11,*

Bâtiment 502, Université Paris Sud, 91405 Orsay Cedex, France.

² *Laboratoire Interactions et Dynamique des Environnements de Surface, UMR 8148 I.D.E.S.,
CNRS-Université Paris-Sud 11, Bâtiment 504, 91405 Orsay Cedex, France.*

³ *Université Pierre et Marie Curie-Paris 6, CNRS,
UMR 7190 (Institut Jean Le Rond d'Alembert), Boite 162, 4 place Jussieu, 75005 Paris, France.*

In an effort to investigate the link between failure mechanisms and the geometry of fractures of compacted grains materials, a detailed statistical analysis of the surfaces of fractured Fontainebleau sandstones has been achieved. The roughness of samples of different widths W is shown to be self affine with an exponent $\zeta = 0.46 \pm 0.05$ over a range of length scales ranging from the grain size d up to an upper cut-off length $\xi \simeq 0.15W$. This low ζ value is in agreement with measurements on other sandstones and on sintered materials. The probability distributions $\pi_{\delta z}(\delta h)$ of the variations of height over different distances $\delta z > d$ can be collapsed onto a single Gaussian distribution with a suitable normalisation and do not display multifractal features. The roughness amplitude, as characterized by the height–height correlation over fixed distances δz , does not depend on the sample width, implying that no anomalous scaling of the type reported for other materials is present. It is suggested, in agreement with recent theoretical work, to explain these results by the occurrence of brittle fracture (instead of damage failure in materials displaying a higher value of $\zeta \simeq 0.8$).

PACS numbers: 62.20.Mk, 46.50.+a, 68.35.Ct

I. INTRODUCTION

The characterization of the geometry of fracture surfaces is of considerable interest for a broad range of practical applications ranging from the hydrology of fractured reservoirs [1, 2] to the derivation of friction laws [3]. Their statistical analysis is also relevant to the understanding of the physics of fracture: The roughness may indeed be expected to reveal failure mechanisms occurring at the microstructure scale [4]. It is now well established that fracture surfaces satisfy a scaling invariance known as *self-affinity* [5, 6, 7, 8, 9, 10]. A *self-affine* profile is one that is statistically invariant under the scaling relation: $z \rightarrow \lambda z$ and $h(z) \rightarrow \lambda^\zeta h(z)$ where the z axis is in the mean fracture plane and normal to the direction of crack propagation, $h(z)$ is the surface height profile and ζ is the self affine exponent. The scaling invariance implies that the probability $\pi_{\delta z}(\delta h)$ to observe a variation of height δh over an horizontal distance δz follow the scaling law:

$$\lambda^\zeta \pi_{\lambda \delta z}(\lambda^\zeta \delta h) = \pi_{\delta z}(\delta h) \quad (1)$$

The prefactor λ^ζ results from the normalization of $\pi_{\delta z}(\delta h)$. As a direct consequence, the height–height correlation function $\Delta h(\delta z)$ satisfies:

$$\Delta h(\delta z) = \langle (h(z + \delta z) - h(z))^2 \rangle_z^{1/2} \propto \delta z^\zeta \quad (2)$$

In many materials including rocks like granite and basalt [7, 8, 9], the roughness exponent ζ was found to be close to 0.8, suggesting at first that it was a *universal* value [5, 6]. However, different exponents were reported for Berea sandstone $\zeta \simeq 0.4 - 0.5$ [11] and then on synthetic sandstone made of sintered glass beads [12]. In this latter case, the exponent ζ is equal to 0.40 ± 0.04 independent of the porosity in the range investigated ($3\% < \phi < 26\%$). This difference raises important fundamental questions regarding the physics of fracture, namely whether ζ is determined by the structure of the material or by the failure mechanism.

In support of the second possibility, a recent work [13] suggests that the value of ζ depends on the existence of a *process zone* where damage processes take place. On the one hand, at length scales smaller than the size of the process zone, fracture surfaces would develop from the growth and coalescence of microdefaults (cracks or voids): This *damage* failure (also called *quasi-brittle* failure) would lead to an exponent $\zeta \simeq 0.8$. On the other hand, at length scales larger than the process zone, the fracture surfaces would result from the continuous propagation of a crack. For this *brittle* failure, the exponent would be $\zeta \simeq 0.4$, reflecting, at the continuum scale, the toughness distribution of the microstructure scale. Two-dimensional numerical simulations realized under these two types of assumptions confirm these results by predicting lower ζ values for brittle fractures [14] than when damage is introduced [15].

While most studies dedicated to the roughness of cracks dealt with surfaces with $\zeta \simeq 0.8$ [5, 6, 7, 8, 9, 10, 16, 17, 18, 19], the present work investigates these

*Present address: COPPE/UFRJ Civil Engineering Program, Rio de Janeiro, RJ 21945-970, Brazil; Electronic address: laurent.r.ponson@wanadoo.fr

†Electronic address: auradou@fast.u-psud.fr

problems through an extensive analysis of the statistical properties of the roughness of fractured Fontainebleau sandstone for which $\zeta \simeq 0.4 - 0.5$.

In addition to the self-affine exponent ζ , another important statistical characteristic is the π distribution of the surface height variations: On granite surfaces ($\zeta = 0.8$), it was found to be Gaussian [19] and a single self-affine exponent was needed to describe the correlation of the surface heights along the crack front direction.

Another important point is the dependence of the roughness statistics on the size of the samples and on the distance to the initiation zone. In the transient propagation region of fractures initiated from a straight notch, the amplitude of the roughness is observed to depend at all length scales on the distance to the initiation [16, 17, 18]. This variation may be described by a so called *anomalous* scaling law involving a new exponent $\zeta_{\text{global}} > \zeta$ referred as the *global* roughness exponent. A consequence of anomalous scaling is expected in regions far from the initiation and where the roughness is fully developed [17, 20]: The roughness amplitude in a window of size δz normal to the crack propagation would then scale with the width W of the fracture surface as:

$$\Delta h(\delta z) \propto \delta z^\zeta W^{\zeta_{\text{global}} - \zeta} \quad (3)$$

In the present study, a statistical analysis of the same type is performed on fractured Fontainebleau sandstone samples of various widths W (perpendicular to the direction of crack propagation). For each surface, the roughness exponent ζ and the range of length scales over which a self-affine description is valid are inferred from the variations of the correlation function Δh with δz . Their dependence on the width W of the samples and on the location on the fracture surface is investigated in order to look for the anomalous scaling features observed on other materials. The probability distribution of the variations of height over given distances δz are also investigated, in order to evaluate the magnitude of multiscaling effects and their dependence on δz .

The differences between these results and the characteristics reported previously for other materials will be discussed and we shall seek to relate them to the failure mechanisms taking place at scales larger than the grain size in Fontainebleau sandstone.

II. SAMPLE CHARACTERIZATION AND EXPERIMENTAL SETUP

The X-Ray analysis of the Fontainebleau sandstone samples used in the present work indicated that they contain 99 % quartz. The size of the grains range from 100 μm to 500 μm with a mean value $d \simeq 270 \mu\text{m}$. 16 SEM micrographs covering a total area of 20 mm \times 20 mm were used to measure the porosity. The pictures are thresholded at a gray level adjusted so as to discriminate between grains and voids. The porosity, defined as the ratio between the void and total areas, is found to be

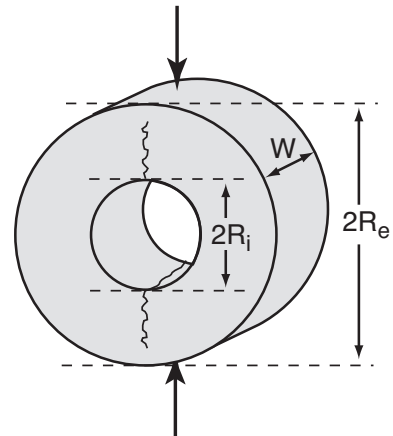


FIG. 1: Schematic view of the toroidal sample (outside radius 60 mm, inside radius 25 mm) and of forces applied during the modified Brazilian test.

$10 \pm 1 \%$.

Slices of widths ranging from $W = 7.8$ to 51.5 mm were sawed off from Fontainebleau paving stones. Toroidal samples were obtained by using hole saws to core out the slices (see Fig. 1). This was achieved by first piercing a circular hole with a 25 mm diameter saw and then a second hole of diameter 60 mm using the same spinning axis. Four slices of widths $W = 7.8, 14.1, 26$ and 51.5 mm were machined and placed in a hydraulic press to perform modified Brazilian fracture tests [21]. The latter is achieved by applying a uniaxial stress at two opposite points on the outside of the torus. The load is increased until two symmetrical cracks propagate from the central hole toward the outside where the compressive forces are applied.

After the failure, one of the fractured blocks is secured to a computer controlled horizontal displacement table. The samples are moved stepwise using steps of lengths Δz (See Tab. I for a detailed list of the actual values.) At each new position, a sensing needle is displaced vertically by a computer controlled microstep motor with a resolution of $\simeq 1 \mu\text{m}$. The contact is detected by a vertical deviation of the needle. The repeatability of the measurement, verified by scanning several times the same profile, is 1 μm . After the detection of the contact, the sensor is raised by 200 μm before the sample is moved laterally again. The sequence is repeated n_z times. Then, the sample is displaced in the perpendicular direction along the x -axis by a step of length Δx and the scanning is repeated again. Finally, one obtains surface maps including $n_z \times n_x$ points. Figure 2 shows one of these maps that displays troughs and bumps with, for the largest, a typical amplitude of the order of one millimeter. In the following, we discuss a detailed statistical analysis of the spatial correlations of the roughness.

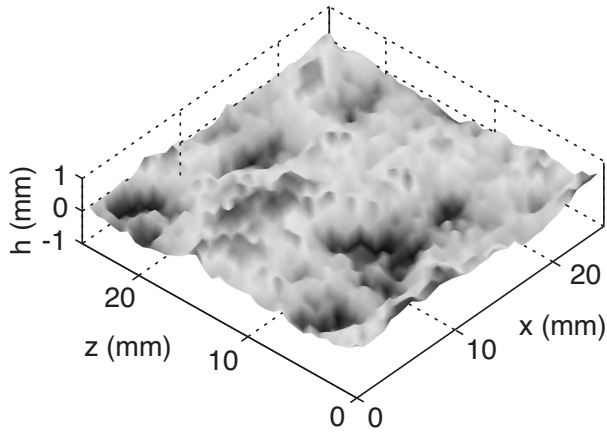


FIG. 2: Topographic image (248×252 pixels) of a fractured sandstone surface with a crack propagation along the x -axis. Sample width: $W = 26$ mm (along the z -axis).

W	Δz	Δx	n_z	n_x	ζ	ζ_{ft}
51.5	50	1000	1007	30	0.51	0.50
26	100	100	248	252	0.48	0.46
14.1	50	250	263	136	0.46	0.43
7.8	25	250	273	133	0.43	0.45

TABLE I: Characteristic parameters of fracture surface geometry. W (mm): specimen width. $\Delta z, \Delta x$ (μm): measurement steps along the z and x . n_z and n_x : number of recorded points along the z and x directions. ζ and ζ_{ft} : self-affine exponents of profiles oriented in the z direction measured respectively using the correlation function and the Fourier power spectrum.

III. EXPERIMENTAL RESULTS

A. Characterization of the surface roughness

We first analyze profiles parallel to the z -axis, *i.e.* normal to the direction of crack propagation, and located far enough from the initiation so that the roughness properties are statistically stationary. The scaling properties of these profiles are characterized by their 1D height–height correlation function $\Delta h(\delta z)$ defined by Eq. (2).

Figure 3 represents in a log-log scale the variations of Δh as a function of the distance δz for one of the samples. Two distinct behaviors are observed: For $\delta z < \xi$, Δh varies as a power law of δz (straight line in a log-log representation) while, for $\delta z > \xi$, Δh remains roughly constant (“plateau domain”). The crossover length scale ξ is, here, defined as the abscissa of the intersection between the power law fit (solid line in Fig. 3) and the plateau variation (dotted horizontal line). The local slope of the correlation function (see inset of Fig. 3) is constant except for δz values smaller than $\simeq 100 \mu\text{m}$: This corresponds roughly to the grain size d which represents therefore a lower boundary of the self affine domain. These results indicate that, at intermediate length scales, the

profiles are self-affine and characterized here by a roughness exponent $\zeta = 0.43$.

The robustness of this self-affine description was verified by using other statistical methods such as the Fourier analysis of the profiles [22]. The exponents obtained in this way are given in Tab. I and are globally independent of the method: Regarding the dependence on W , a global increasing trend is observed but the total variation is very weak, less than 0.1, which is of the same order as the interval of confidence on the value of one exponent estimated for a given width. The self-affine exponent obtained after averaging over all data is $\zeta = 0.46 \pm 0.05$. Applying the same analysis to profiles parallel to the x direction, *i.e.* the direction of crack propagation, leads to a self-affine exponent equal to 0.49 ± 0.05 . These observations are consistent with measurements performed on other natural and artificial sandstones [11, 12, 13].

For δz larger than ξ , the variations of Δh level off indicating that the surface is flat at large scales. In order to test the robustness of the value of ξ with respect to possible bias introduced by the statistical analysis, the computation was repeated on data sets including only one out of two data points. The value of the cut-off length remained the same. Finally, the same procedure was applied in different regions of the surface. Each of the surfaces was divided into three regions of equal width $W/3$. Two of these subsurfaces are thus on the sides of the sample while the third one covers the central region. In Fig. 3, correlation functions Δh computed on the central (\times) and on one of the lateral (\cdot) subregions are overlaid. All curves fall on top of each other, showing that the crossover length ξ is independent of the region

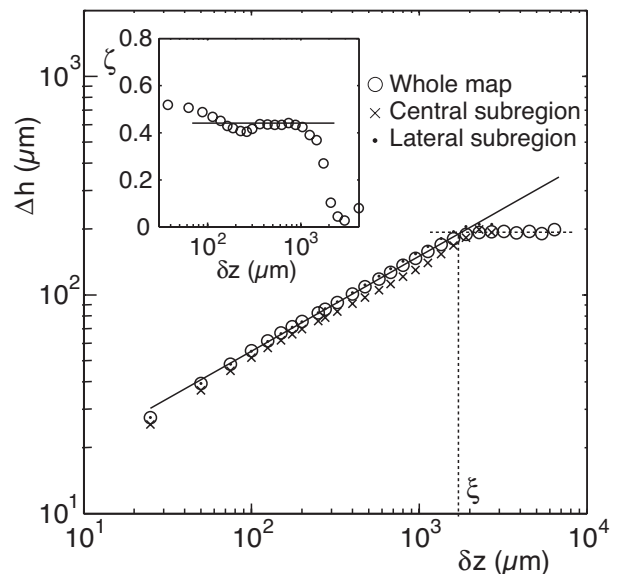


FIG. 3: Log-log representation of the height–height correlation function Δh as a function of δz computed along the crack front direction (z -axis) for a sample of width $W = 7.8$ mm. Straight line: Linear regression of the data for $\delta z < \xi$ with slope $\zeta = 0.43$. Inset: Local slope of the correlation function.

of the fracture surface. Therefore, ξ is a relevant length scale of the problem which reflects neither an influence of the sides of the sample nor of the sampling period of the surface maps.

Before studying the scaling behavior of ξ with the sample width, we analyze now the distribution $\pi_{\delta z}$ of the variations of height.

B. Statistical distribution of the fluctuations of height

For each sample, a scan including at least 30,000 measurement points has been performed. Such a large data set allows one to compute with a good accuracy the probability distributions $\pi_{\delta z}(\delta h)$ for values of δz ranging from the typical grain size up to several times the grain diameter. Fig. 4 displays such probability distributions corresponding to several δz values ranging from $300 \mu\text{m}$ to 1.3 mm , i.e. larger than the mean grain diameter d .

For self-affine profiles, one expects $\pi_{\delta z}$ to satisfy Eq. (1), valid for any scaling parameter λ . Using the particular value $\lambda = 1/\delta z$, this equation becomes :

$$\pi_{\delta z}(\delta h) = \left(\frac{1}{\delta z}\right)^\zeta \pi\left(\frac{\delta h}{\delta z^\zeta}\right) \quad (4)$$

Therefore, using the normalized variable $u = \delta h/\delta z^\zeta$, all the distributions $\delta z^\zeta \pi_{\delta z}$ should collapse onto a same master curve $\pi(u)$, at least for δz values pertaining to the self-affine regime. Such a collapse is indeed observed in Figure 4: The same data as in the insert have been plotted in these normalized coordinates using the roughness exponent $\zeta = 0.43$ measured from the scaling of the correlation function (see Fig. 3).

One of the key consequence of this precise collapse is that all moments $\langle (h(z + \delta z) - h(z))^p \rangle^{1/p}$ of order $p > 1$ of the $\pi_{\delta z}$ distributions must scale as δz^ζ . This is a clear evidence of the lack of multiscaling of the surface investigated. In other words, the single exponent ζ is enough to describe the full statistics of the variations of height on the fracture surface along the z -axis, at least in the range of length scales $d < \delta z < \xi$.

Let us now focus on the master curve $\pi(u)$ which has the characteristic bell-like shape of Gaussian distributions. This is more precisely demonstrated in the semi-logarithmic plot of Fig. 5 in which a Gaussian curve (continuous line) with a second moment equal to one is observed to coincide with the experimental data sets corresponding to $\delta z \geq 300 \mu\text{m}$, i.e. $\delta z \geq d$. The statistical properties of the surface are therefore fully described by this Gaussian distribution and by the single roughness exponent $\zeta = 0.43$.

We have also represented the $\pi_{\delta z}$ -distributions corresponding to length scales smaller than the mean grain diameter $d = 270 \mu\text{m}$, namely $\delta z = 75$ and $150 \mu\text{m}$. They clearly do not collapse with the other curves although their second moment was shown to scale roughly

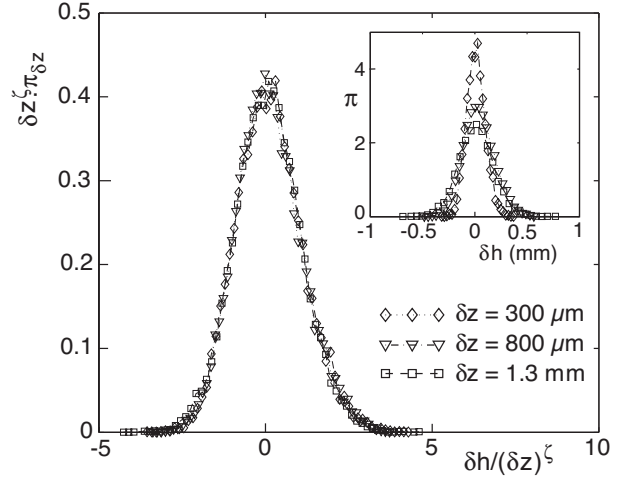


FIG. 4: Probability distribution of height variations over a distance δz normalized using Eq.(4) with $\zeta = 0.43$ as obtained by the analysis of the second moment Δh of the height distribution (See Sec. III A). δh and δz have been normalized by a same length scale $\ell = 35 \mu\text{m}$ chosen so that the second moment of the normalized distributions is equal to 1. Inset : Plot in linear coordinates of $\pi_{\delta z}(\delta h)$ for $300 \mu\text{m} \leq \delta z \leq 1.3 \text{ mm}$.

as δz^ζ in this range of scales (see Fig. 3). It means that, in the domain of small distances ($\delta z < d$), the $\pi_{\delta z}$ distributions are not Gaussian and their moments cannot be rescaled with a single exponent. In this range of δz values, it would be possible to rescale all the moments $\langle (h(z + \delta z) - h(z))^p \rangle^{1/p}$ by using several exponents ζ_p

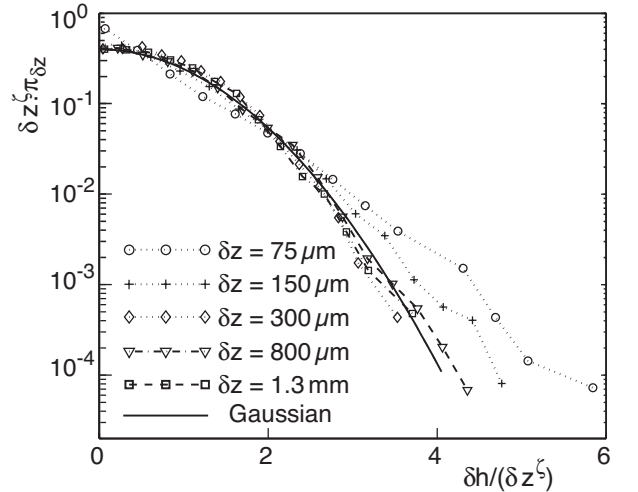


FIG. 5: Probability density $\pi_{\delta z}(u)$ in a semi-logarithmic representation for $75 \mu\text{m} \leq \delta z \leq 1.3 \text{ mm}$. Here $u = \frac{\delta h}{\ell} \frac{\ell^\zeta}{\delta z^\zeta}$ with $\ell = 35 \mu\text{m}$ and $\zeta = 0.43$ as obtained from the analysis of the second moment of the distribution (See Sec.III A). For clarity only positive u are displayed. Continuous line : Gaussian distribution $\frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}}$.

(not shown here): The relevance of such a multiscaling description at length scales for which the geometry of a single grain has a predominant effect is however questionable.

These results bring new insight to a recently debated question concerning crack lines resulting from the rupture of paper sheets that were found to exhibit multiscaling [23], at least at small scales, *i.e.* at length scales comparable with the length of the fibers of the paper. Other observations, performed on the same material, but over a wider range of length scales, reported that, at larger scales, there was a crossover from this multiscaling behavior towards a self-affine one [19]. These results may have similarities with our experiments, even though they correspond to the 3D rupture of a very different material: In our case, the crossover length correspond to the mean grain diameter d of the sandstone specimen.

C. Dependence of the statistical properties on the sample width

In addition to the lower limit of the order of the grain diameter d discussed above, the self-affine domain has also an upper limit ξ (see Figure 3) which generally depends on the sample size. For granite, the experimental upper limit ξ is of the order of one fourth of the specimen size [24, 25]. For mortar, the geometry can be considered as self-affine only up to length scales of the order of 15 % of the specimen width W [18]. A systematic study of wood samples with various values of W leads to $\xi = 0.1 W$ [17].

Figure 6 displays the variations of the correlation function $\Delta h(\delta z)$ as a function of δz for samples of different widths W . All data sets display a self-affine domain followed by a plateau region corresponding to a value of $\Delta h(\delta z > \xi)$ increasing with W ; the upper limit ξ of the self-affine domain also clearly increases with the system size. The variation of ξ with W is plotted in Figure 7 and is well fitted by a straight line of slope 0.15 going through the origin.

A value of the upper limit of the self-affine domain for profiles parallel to the direction x of crack propagation is also plotted in Figure 7 (\diamond). This length is, in this case, the average of values of ξ determined for four samples of different widths and the error bar reflects the variability of the values. In order to plot this result in Figure 7, these profiles have been assumed to correspond to a value of W equal to 35 mm (*i.e.* the length of the samples along the x direction). The corresponding data point is consistent with the linear fit corresponding in Figure 7 to profiles parallel to the z -axis. The scaling relation between ξ and the system width W established above seems apparently also applicable in the x direction.

Let us now compare the surface roughness in the self-affine domain at length scales between d and ξ with the anomalous scaling characteristics recently observed [16, 17, 18]. Anomalous growth implies that, after a transient

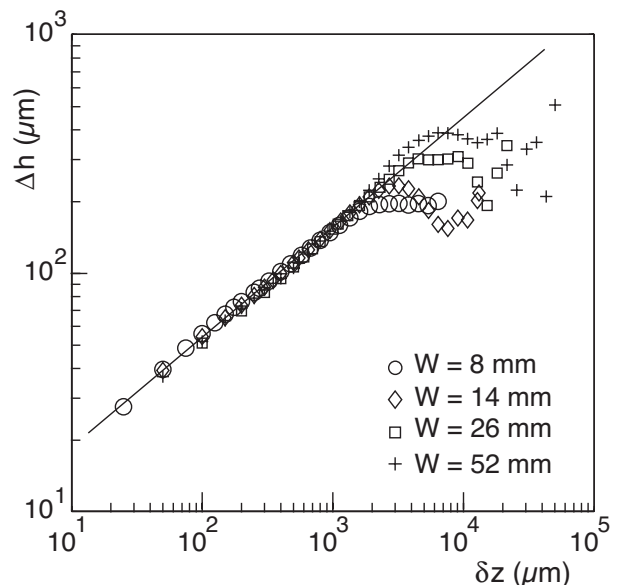


FIG. 6: Log-log representation of the height–height correlation function $\Delta h(\delta z)$ computed along the z -axis for 4 specimens of different widths W . The straight line is a linear regression of slope $\zeta = 0.47$.

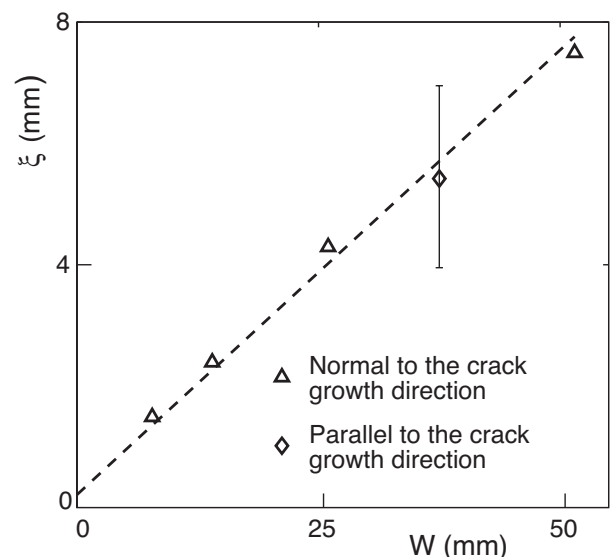


FIG. 7: Variations of the correlation length ξ_z (\triangle) (resp. ξ_x (\diamond)) as a function of the specimen width (resp. length) W . Slope of the dashed line: 0.15.

regime, the roughness amplitude $\Delta h(\delta z = cst < \xi)$ scales as $W^{\zeta_{global} - \zeta}$ with the system width W (see Eq.(3)). All the profiles analyzed correspond to the stationary propagation domain in order to make the comparisons meaningful. The extent of the transient domain near the crack initiation has been found in various materials to be of the order of few millimeters [12, 18]. Here, a value close to ~ 2 mm was measured and all profiles considered in the present work are outside this region.

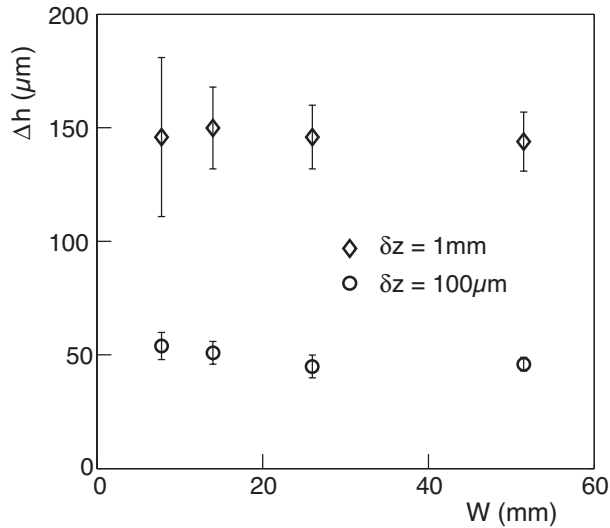


FIG. 8: Height–height correlation function $\Delta h(\delta z)$ for fixed values of δz as a function of the specimen width W . (\diamond): $\delta z = 1$ mm; (\circ): $\delta z = 100 \mu\text{m}$. Error bars: Standard deviation of $\Delta h(\delta z)$.

The height–height correlation function is plotted in Fig. 8 as a function of the specimen width W for two different window sizes δz . In contrast with the predictions of Eq. (3) for anomalous scaling, the roughness amplitude $\Delta h(\delta z < \xi)$ in the self-affine domain is independent of W over a range of variations of almost 1 to 10 (the same conclusions may already be inferred from Fig. 6 but the sensitivity is better here due to the linear scale). These characteristics differ therefore completely from those expected for anomalous scaling.

IV. DISCUSSION AND CONCLUSIONS

Let us now discuss the origin of the statistical properties observed for the present Fontainebleau sandstone surfaces. In a recent study, Bonamy *et al.* [13] analyzed the fracture surfaces morphology in glassy materials, *i.e.* homogeneous silica glass and sintered glass. They suggest that, on the one hand, higher exponents $\zeta \sim 0.8$ reflect damage failure processes occurring in a zone surrounding the crack tips and are observable at length scales smaller than the size of the process zone; on the other hand, low roughness exponents $\zeta \sim 0.4$ would result from brittle fracture and be observable either in experiments where no process zone develops or at length scales larger than the size of the process zone. In this perspective, and as is discussed in more detail below, the low value $\zeta \simeq 0.45$ reported here for Fontainebleau sandstone samples is the signature of brittle fracture; moreover, since it is observed at length scales down to the grain size, no process zone is present in these experiments.

In spite of these important differences, surfaces obtained from brittle and quasi-brittle failures share com-

mon features. In both cases, a single exponent is enough to describe the scaling invariance of the roughness [19]: this confirms the relevance of the self-affine description of fracture surfaces for both types of materials.

The lack of anomalous scaling in the present fracture surfaces compared to materials such as concrete, wood or granite displaying damage failure is an other indication that no damage process occurs in our experiments. In these latter studies, confinement effects limit the development of the process zone: Its extension and internal structure are then set by the system size W when a stationary propagation regime is reached. As a result, from Eq. (3) [16], the roughness amplitude $\Delta h(\delta z = cst)$ varies with W as $\Delta h(\delta z = cst) \propto W^{\zeta_{\text{global}} - \zeta}$ as is indeed observed experimentally [20]. In contrast, in the absence of a process zone, $\Delta h(\delta z = cst)$ is only set by the microstructural and mechanical properties of the material and does not depend on the system size (see for instance the model of Refs. [13, 26]) as observed experimentally here.

The same type of approach accounts for the domains of observation of the different self-affine geometries. For damage fractures, the upper bound ξ of the self-affine domain where $\zeta \sim 0.8$ is set by the size of the process zone [10, 13] or by the sample size W if it is smaller than the process zone. In the present case of a brittle fracture with no process zone, the lower boundary of the self-affine domain is set by the grain size. The upper cut-off length ξ increases linearly with the sample size W : in this case, no other characteristic length than W seems to determine ξ so that it might increase indefinitely with W . These results suggest that the two different self affine geometries might coexist on a same fracture surface: the characteristic exponent would have a value $\zeta \simeq 0.8$ for lengths scales up to the size of the process zone and a value $\zeta \simeq 0.4$ at larger length scales up to the plateau domain where $\Delta h(\delta z)$ becomes constant.

A key issue is whether the development of a process zone is purely material dependent. Recent experiments [27, 28] suggest that fractured samples made of cemented grains, and therefore similar to Fontainebleau sandstone, do not always display brittle failure. The emission of acoustic waves was measured during the growth of a crack initiated from a chevron shaped notch under fatigue in a Permian sandstone sample. The localization of the acoustic events during failure allowed to demonstrate that a process zone was present and to determine its size $\ell_{pz} \simeq 25$ mm and its spatio-temporal evolution [27]. Moreover, the morphology of the resulting fracture surfaces [28] was found to be self-affine for length scales less than 10 mm ($< \ell_{pz}$) and characterized by an exponent $\zeta = 0.75 \pm 0.03$, similar to the usual value for materials displaying damage fractures. This observation supports the assertion of Ref. [13] and shows that the roughness exponent depends not only on the material, but also on the experimental conditions (geometry of initiation notch, loading mode...)

To conclude, the present experimental results and their

comparison to previous works indicate that the value of the self-affine exponent ζ is a clear signature of the failure mode : damage fracture involving a process zone if $\zeta \simeq 0.8$ or brittle fracture if $\zeta \simeq 0.4$. Another characteristic signature of damage fracture is anomalous scaling marked by a variation of the roughness amplitude with the sample size (if the latter is smaller than the process zone). The range of length scales over which the fracture geometry is self-affine with a given exponent ζ may represent an important additional information. For $\zeta \simeq 0.8$, this range should extend from the size of the grains to that of the process zone (which may be limited by the sample size); for $\zeta \simeq 0.4$, it may extend from the size of the grains (if there is no process zone) or that of the process zone up to a length scaling as the size of the specimen.

An important test of these hypothesis will then be to force the development of a process zone in materials of the type used here by modifying the loading or the geometry of the experiments. For instance, one may use an initial chevron notch geometry as in refs. [27, 28], where damage processes occur (so that $\zeta = 0.8$) although the

material is similar to the Fontainebleau sandstone used here. If a transition from brittle to damage fracture is induced in this way, this would result in a variation of the self affine exponent ζ or in the coexistence of two self-affine domains with $\zeta \simeq 0.8$ below the size of the process zone and $\zeta \simeq 0.4$ above it.

Acknowledgments

We are indebted to G. Chauvin, R. Pidoux (FAST) and J.P. Villote, V. Godard (IDES) for their assistance in the realization of the experimental set-up. We are grateful to E. Bouchaud, D. Bonamy, J.P. Bouchaud, A. Hansen and K.J. Måløy for their enlightening comments. This work is supported by the CNRS and ANDRA through the GdR FORPRO - the EHDRA (European Hot Dry Rock Association) - the PNRH programs and the Paris XI university through a PPF. L. P. is partially supported by the French Ministry of Foreign Affairs (Lavoisier Program).

-
- [1] P. M. Adler and J.-F. Thovert, *Fractures and Fracture Networks* (kluwer Academic Publishers, 1999).
 - [2] R. Zimmerman and I. Main, in *Mechanics of Fluids-Saturated Rocks*, edited by Y. Guéguen and M. Boutéca (Elsevier Academic Press, 2004).
 - [3] B. K. Chakrabarti, *Modelling Critical and Catastrophic Phenomena in Geoscience: A Statistical Physics Approach* (Springer, 2005).
 - [4] E. Bouchaud, Surf. Rev. Lett. **10**, 797–814 (2003).
 - [5] E. Bouchaud, G. Lapasset, and J. Planès, Europhys. Lett. **13**, 73 (1990).
 - [6] K. J. Måløy, A. Hansen, E. L. Hinrichsen, and S. Roux, Phys. Rev. Lett. **68**, 213 (1992).
 - [7] C.Y. Poon, R.S. Sayles, and T.A. Jones, J. Phys. D: Appl. Phys. **25**, 1269–1275 (1992).
 - [8] J. Schmittbuhl, S. Gentier, and S. Roux, Geophys. Res. Lett. **20**, 639 (1993).
 - [9] J. Schmittbuhl, F. Schmitt, and C. Scholz, J. Geophys. Res. **100**, 5953 (1995).
 - [10] L. Ponson, D. Bonamy, and E. Bouchaud, Phys. Rev. Lett. **96**, 035506 (2006).
 - [11] J. M. Boffa, C. Allain, and J. P. Hulin, Eur. Phys. J. Appl. Phys. **2**, 281 (1998).
 - [12] L. Ponson, H. Auradou, P. Vié, and J. P. Hulin, Phys. Rev. Lett. **97**, 125501 (2006).
 - [13] D. Bonamy, L. Ponson, S. Prades, E. Bouchaud, and C. Guillot, Phys. Rev. Lett. **97**, 135504 (2006).
 - [14] E. Katzav, M. Adda-Bedia, and B. Derrida, to appear in Europhysics Lett., arXiv:cond-mat/0610185v1 (2007).
 - [15] E. Bouchbinder, J. Mathiesen, and I. Procaccia, Phys. Rev. Lett. **92**, 245505 (2004).
 - [16] J. M. Lopez and J. Schmittbuhl, Phys. Rev. E **57**, 6405 (1998).
 - [17] S. Morel, J. Schmittbuhl, J. M. Lopez, and G. Valentin, Phys. Rev. E **58**, 6999 (1998).
 - [18] G. Mourot, S. Morel, E. Bouchaud, and G. Valentin, Phys. Rev. E **71**, 016136 (2005).
 - [19] S. Santucci, K. J. Måløy, A. Delaplace, J. Mathiesen, A. Hansen, J. Bakke, J. Schmittbuhl, L. Vanel, and P. Ray, Phys. Rev. E **75**, 016104 (2007).
 - [20] G. Mourot, S. Morel, E. Bouchaud, and G. Valentin, Int. J. Frac. **140**, 39–54 (2006).
 - [21] F. L. L. B. Carneiro and A. Barcellos, Bulletin RILEM **1**, 97 (1953).
 - [22] J. Feder, *Fractals* (Plenum, 1988).
 - [23] E. Bouchbinder, I. Procaccia, S. Santucci, and L. Vanel, Phys. Rev. Lett. **96**, 055509 (2006).
 - [24] Y. Méheust and J. Schmittbuhl, Geophys. Res. Lett. **27**, 2989 (2000).
 - [25] H. Auradou, G. Drazer, J. P. Hulin, and J. Koplik, Water Resour. Res. **41**, 3938 (2005).
 - [26] L. Ponson, Ph.D. thesis, Ecole Polytechnique (2006).
 - [27] T. Backers, S. Stanchits, and G. Dresen, Int. J. Rock Mech. Min. Sc. **42**, 1094 (2005).
 - [28] T. Backers, N. Fardin, G. Dresen, and O. Stephansson, Int. J. Rock Mech. Min. Sc. **40**, 425 (2003).